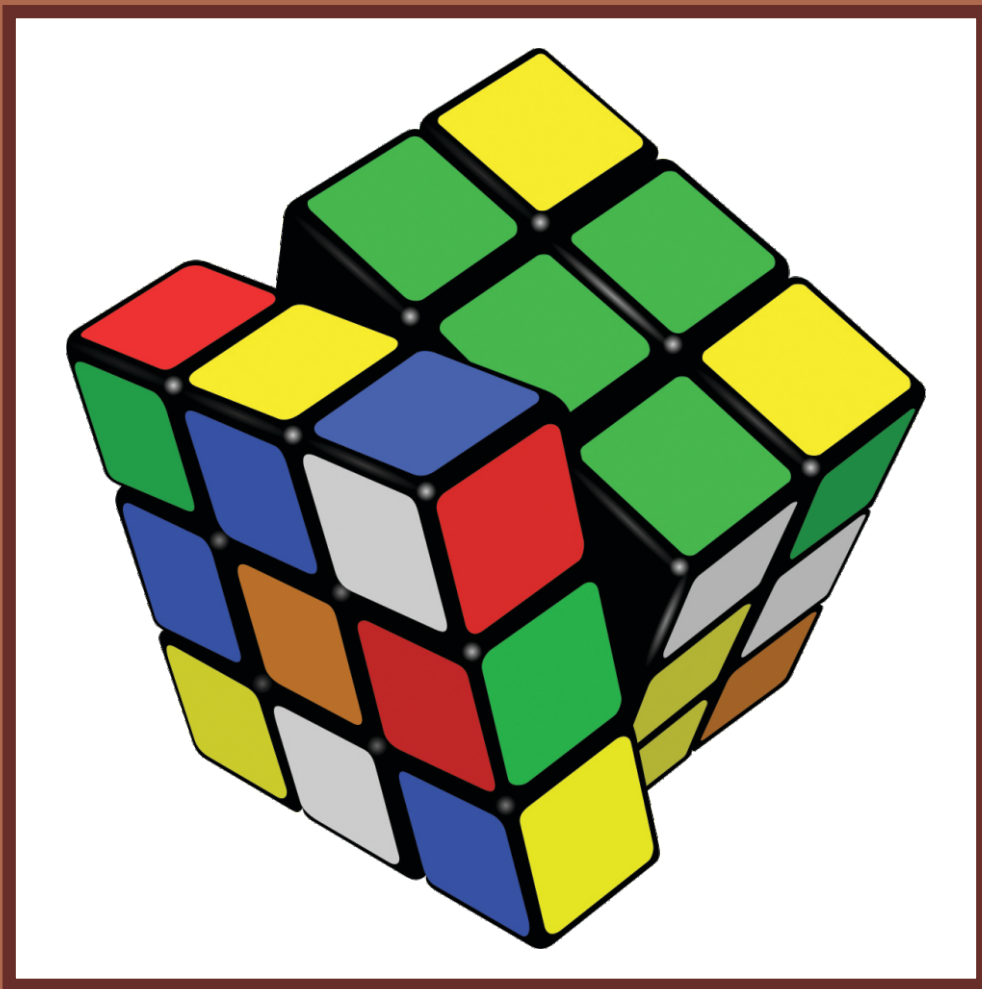


# Fundamental of **Abstract Algebra**



**Dr. Subhashish Biswas**  
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# **Fundamental of Abstract Algebra**

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